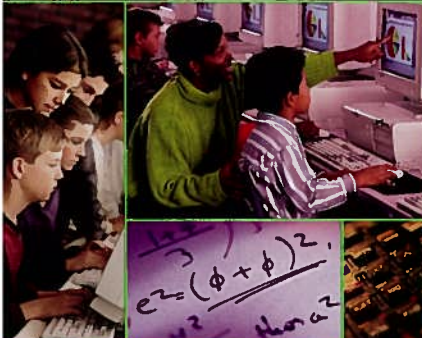


Principles and Standards  
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# Navigating *through* Geometry *in* Grades 6–8



NATIONAL COUNCIL OF  
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# Geometry

## Navigating through Geometry in Grades 6–8

By David K. Pugalee, Jeffrey Frykholm, Art Johnson, Hannah Slovin, Carol Malloy,  
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