

Given: Nitrogen in a closed, rigid tank



$$T_1 = 440^\circ\text{F}$$

$$p_1 = 14.5 \text{ psia}$$

$$p_2 = 50 \text{ psia}$$

Find: T_2 , Δu using a) The ideal gas model
b) The real-fluid model

Solution: a) Using the ideal gas model,

$$\left. \begin{array}{l} p_1 v_1 = RT_1 \\ p_2 v_2 = RT_2 \end{array} \right\} v_2 = v_1 \text{ therefore } T_2 \text{ can be found!}$$

$\Delta u = u_2 - u_1$ The ideal gas Δu can be found using 'N2' as the fluid in EES!

b) Using the real fluid model,

$$\left. \begin{array}{l} p_1 = p(v_1, T_1) \\ p_2 = p(v_2, T_2) \end{array} \right\} v_2 = v_1 \text{ Therefore } T_2 \text{ can be found!}$$

$\Delta u = u_2 - u_1$ The real-fluid Δu can be found using 'nitrogen' as the fluid in EES!



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GIVEN: Nitrogen in a closed, rigid tank

$$T_1 = 440 \text{ [F]}$$

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$$p_2 = 50 \text{ [psia]}$$

FIND: T_2 and the change in internal energy of the nitrogen using the ideal gas model and the real fluid model. How do they compare? (Refelction)

SOLUTION:

(a) - The ideal gas properties for nitrogen can be accessed using the fluid 'N2'

The final temperature can be found by equating the specific volumes at states 1 and 2

$$v_{1,i} = v \text{ ['N2', } T = T_1, P = p_1 \text{]}$$

$$v_{2,i} = v_{1,i}$$

$$v_{2,i} = v \text{ ['N2', } T = T_{2,i}, P = p_2 \text{]}$$

The change in internal energy of the nitrogen is,

$$u_{1,i} = u \text{ ['N2', } T = T_1 \text{]}$$

$$u_{2,i} = u \text{ ['N2', } T = T_{2,i} \text{]}$$

$$\Delta u_i = u_{2,i} - u_{1,i}$$

(b) - The real fluid properties for nitrogen can be found using fluid 'nitrogen'

$$v_{1,r} = v \text{ ['Nitrogen', } T = T_1, P = p_1 \text{]}$$

$$v_{2,r} = v_{1,r}$$

$$v_{2,r} = v \text{ ['Nitrogen', } T = T_{2,r}, P = p_2 \text{]}$$

The change in internal energy of the nitrogen using real fluid behavior is,

$$u_{1,r} = u \left[\text{'Nitrogen'} , T = T_1 , P = p_1 \right]$$

$$u_{2,r} = u \left[\text{'Nitrogen'} , T = T_{2,r} , P = p_2 \right]$$

$$\Delta u_r = u_{2,r} - u_{1,r}$$

SOLUTION

Unit Settings: Eng F psia mass deg

$$\Delta u_i = 462.9 \text{ [Btu/lb}_m\text{]}$$

$$p_1 = 14.5 \text{ [psia]}$$

$$T_1 = 440 \text{ [F]}$$

$$T_{2,r} = 2642 \text{ [F]}$$

$$u_{1,r} = 159.9 \text{ [Btu/lb}_m\text{]}$$

$$u_{2,r} = 622.9 \text{ [Btu/lb}_m\text{]}$$

$$v_{1,r} = 23.78 \text{ [ft}^3\text{/lb}_m\text{]}$$

$$v_{2,r} = 23.78 \text{ [ft}^3\text{/lb}_m\text{]}$$

$$\Delta u_r = 463 \text{ [Btu/lb}_m\text{]}$$

$$p_2 = 50 \text{ [psia]}$$

$$T_{2,i} = 2643 \text{ [F]}$$

$$u_{1,i} = 26.83 \text{ [Btu/lb}_m\text{]}$$

$$u_{2,i} = 489.7 \text{ [Btu/lb}_m\text{]}$$

$$v_{1,i} = 23.77 \text{ [ft}^3\text{/lb}_m\text{]}$$

$$v_{2,i} = 23.77 \text{ [ft}^3\text{/lb}_m\text{]}$$

No unit problems were detected.

KEY VARIABLES

$$T_{2,i} = 2643 \text{ [F]}$$

(a) T_2 using the ideal gas model

$$\Delta u_i = 462.9 \text{ [Btu/lb}_m\text{]}$$

(a) change in internal energy using the ideal gas model

$$T_{2,r} = 2642 \text{ [F]}$$

(b) T_2 using the real fluid model

$$\Delta u_r = 463 \text{ [Btu/lb}_m\text{]}$$

(b) change in internal energy using the real fluid model

REFLECTION:

Nitrogen (and many other substances) are included in EES as ideal gases AND real fluids! Using the ideal gas fluid, there is no need to write out the ideal gas EOS! It is contained in the property call.

In this case, the ideal gas model and the real fluid model give answers that are very close! This means that the ideal gas model appears to be a valid approximation to the real fluid behavior for this problem.

Did you notice that the *absolute* values of u_1 and u_2 for the two models are not the same? For example, $u_{1_i} = 26.83[\text{Btu/lbm}]$ and $u_{1_r} = 159.9[\text{Btu/lbm}]$! However, when you look at the *change* in internal energy, the values are nearly the same!!