Rules:

1. $0 \leq P\left(x_{i}\right) \leq 1$
2. $\sum P\left(x_{i}\right)=1$
3. Complement: $P\left(A^{\prime}\right)=1-P(A)$
4. Addition: $P(A$ or $B)=P(A)+P(B)-P(A$ and $B)$
5. Multiplication (independent only): $P(A$ and $B)=P(A) P(B)$

## Confusion matrix

$d=P(A$ and $B), e=P\left(A\right.$ and $\left.B^{\prime}\right), f=P(A), g=P\left(A^{\prime}\right.$ and $\left.B\right), h=P\left(A^{\prime}\right.$ and $\left.B^{\prime}\right), i=P\left(A^{\prime}\right)$, $j=P(B), k=P\left(B^{\prime}\right)$

|  | $P(B)$ | $P\left(B^{\prime}\right)$ |  |
| :---: | :---: | :---: | :---: |
| $P(A)$ | d | e | f |
| $P\left(A^{\prime}\right)$ | g | h | i |
|  |  |  |  |
|  | j | k | 1 |

EXAMPLE1: How accurate are the weather predictions? Look at weather predictions and actual weather for one calendar year (365 days).

Data is a mix of a contingency table with probability example

|  | A rain | A no rain |  |
| :---: | :---: | :---: | :---: |
| F Rain | 27 | 63 | 90 |
| F no rain | 7 | 268 | 275 |
|  | 34 | 331 | 365 |

$P($ Forecasted rain $)=\frac{90}{365}=0.2466$
$P($ Forecasted no rain $)=\frac{275}{365}=0.7534$
$P($ forecast rain and no actual rain $)=\frac{63}{365}=0.1726$
$56 \%$ of American workers have a retirement plan, $68 \%$ have health insurance, and $49 \%$ have both.
$P(R P)=0.56, P(H I)=0.68, P(R P$ and $H I)=0.49$

|  | $P(H I)$ | $P\left(H I^{\prime}\right)$ |  |
| :---: | :---: | :---: | :---: |
| $P(R P)$ | 0.49 | 0.07 | 0.56 |
| $P\left(R P^{\prime}\right)$ | 0.19 | 0.25 | 0.44 |
|  | 0.68 | 0.32 | 1 |

$P\left(R P^{\prime}\right.$ and $\left.H I^{\prime}\right)=0.25$
$P\left(R P^{\prime}\right.$ or $\left.H I^{\prime}\right)=P\left(R P^{\prime}\right)+P\left(H I^{\prime}\right)-P\left(R P^{\prime}\right.$ and $\left.H I^{\prime}\right)=0.44+0.32-0.25=0.51$
Are RP and HI mutually exclusive? NO because the intersection between RP and HI exists (they can happen at the same time)

Are RP and HI independent? $P(R P$ and $H I) ?=? P(R P) P(H I) \Rightarrow 0.49 ?=?(0.56)(0.68) \Rightarrow$ $0.49 \neq 0.3808 \therefore \mathrm{RP}$ and HI are not independent (they are dependent)

